

Proof:

Pick $x, y \in G$ such that $f(x) = f(y)$, we will show that $x = y$

$$f(x) = f(y)$$

$$g * x = g * y$$

By left cancellation law, we get

$$x = y \text{ (Q.E.D)}$$

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